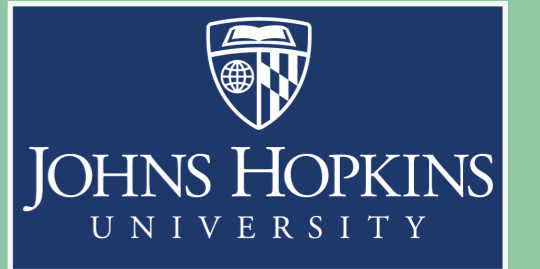
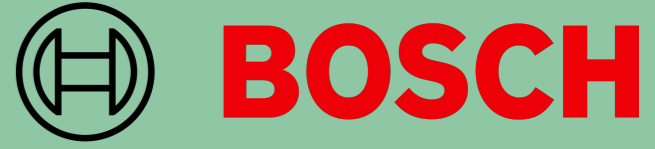


# Fast yet Safe: Early-Exiting with Risk Control



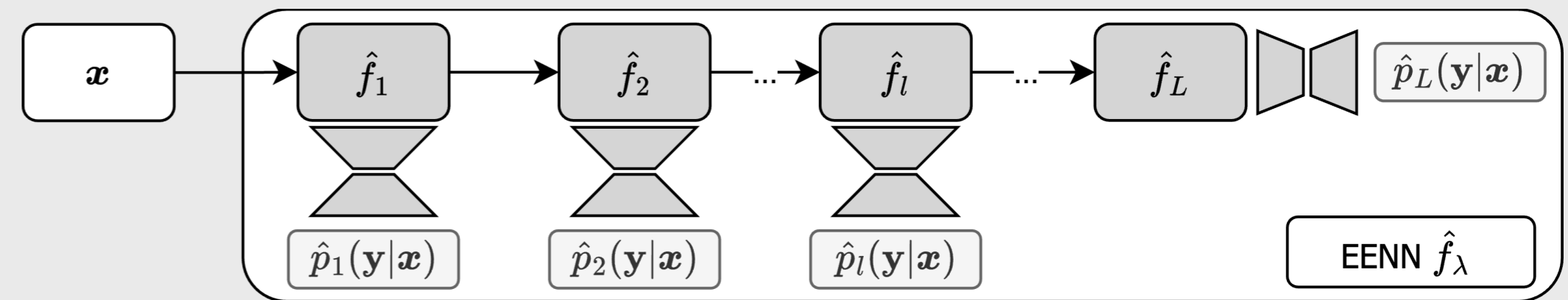
Metod Jazbec<sup>1,\*</sup> Alexander Timans<sup>1,\*</sup> Tin Hadži Veljković<sup>1</sup>  
 Kaspar Sakmann<sup>2</sup> Dan Zhang<sup>2</sup> Christian A. Naeseth<sup>1</sup> Eric Nalisnick<sup>1,3</sup>  
 — <sup>1</sup> University of Amsterdam <sup>2</sup> BCAI <sup>3</sup> Johns Hopkins University —

## Motivation

Model inference should be dynamic based on user or data conditions. A simple yet effective solution is to permit intermediate exiting of model layers (EENNs).

- Problem: How to select the EENN's exit condition  $\lambda$  to balance the performance vs. efficiency trade-off.
- Solution (TLDR): Employ post-hoc, distribution-free risk control to resolve the trade-off according to user specifications with statistical guarantees.

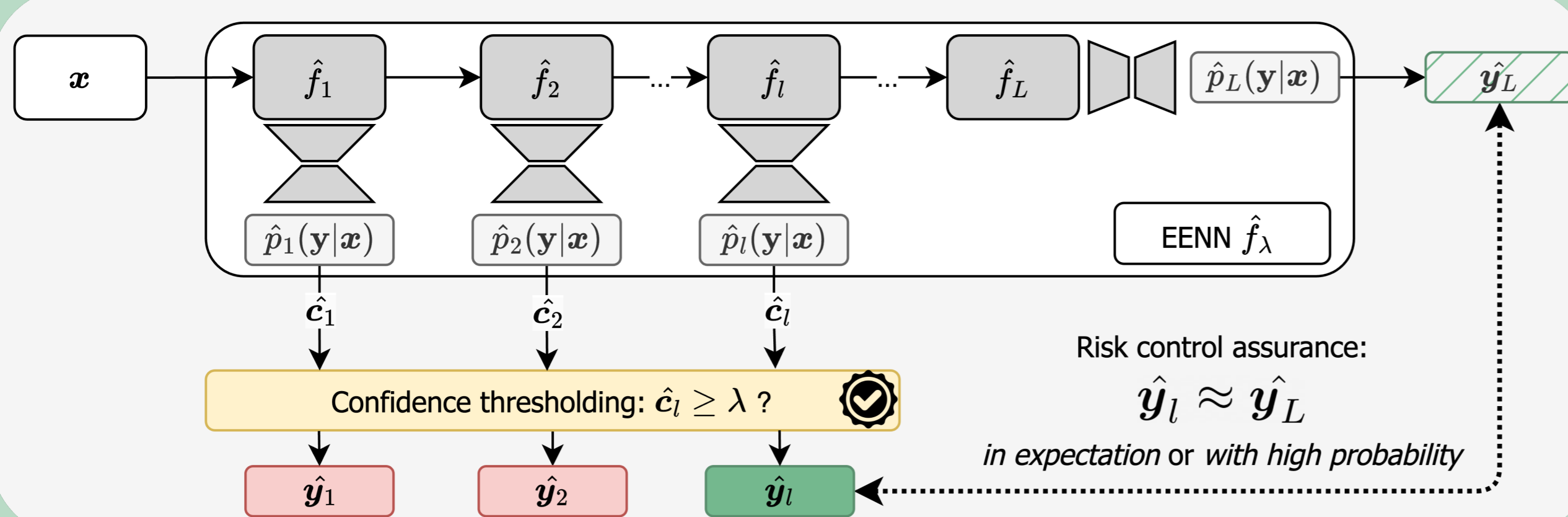
## Early-Exit Neural Networks (EENNs)



Marginal monotonicity assumption:

$$\mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim \mathcal{P}}[\ell(\hat{p}_l(\mathbf{y}|\mathbf{x}), \mathbf{y})] \geq \mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim \mathcal{P}}[\ell(\hat{p}_{l+1}(\mathbf{y}|\mathbf{x}), \mathbf{y})] \quad \forall l = 1, \dots, L-1$$

## Early-Exiting with Risk Control



Empirical threshold:  $\hat{\lambda}_{\text{emp}} := \min\{\lambda \in \Lambda : \hat{\mathcal{R}}(\lambda; \mathcal{D}_{\text{cal}}) \leq \epsilon\}$

► No guarantees !

Conformal Risk Control (CRC):  $\hat{\lambda}_{\text{CRC}} := \min\left\{\lambda \in \Lambda : \frac{n}{n+1}\hat{\mathcal{R}}(\lambda; \mathcal{D}_{\text{cal}}) + \frac{B}{n+1} \leq \epsilon\right\}$

► Risk control in expectation:  $\mathbb{E}_{\mathcal{D}_{\text{cal}} \sim \mathcal{P}^n}[\mathcal{R}(\hat{\lambda}_{\text{CRC}})] \leq \epsilon$

Upper Confidence Bound (UCB):  $\hat{\lambda}_{\text{UCB}} := \min\{\lambda \in \Lambda : \hat{\mathcal{R}}^+(\lambda'; \mathcal{D}_{\text{cal}}) < \epsilon, \forall \lambda' \geq \lambda\}$

► Risk control w. high probability:  $\mathbb{P}_{\mathcal{D}_{\text{cal}} \sim \mathcal{P}^n}(\mathcal{R}(\hat{\lambda}_{\text{UCB}}) \leq \epsilon) \geq 1 - \delta$

## Framework

### INPUT

- Exit threshold candidates  $\lambda \in [0, 1]$
- Early-exit risk of the form  $\mathcal{R}(\lambda) = \mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim \mathcal{P}}[\ell(\hat{\sigma}_\lambda(\mathbf{x}), \mathbf{y}) - \ell(\hat{\sigma}_L(\mathbf{x}), \mathbf{y})]$ ,  $\hat{\sigma}_l(\mathbf{x}) = \hat{y}_l$  or  $\hat{\sigma}_l(\mathbf{x}) = \hat{p}_l(\mathbf{y}|\mathbf{x})$
- User-defined risk settings  $\ell : \mathcal{Y} \times \mathcal{Y} \rightarrow \mathbb{R}, \epsilon \in (0, 1), \delta \in (0, 1)$

### OUTPUT

- Risk-controlling exit threshold  $\hat{\lambda} \in [0, 1]$

## Options

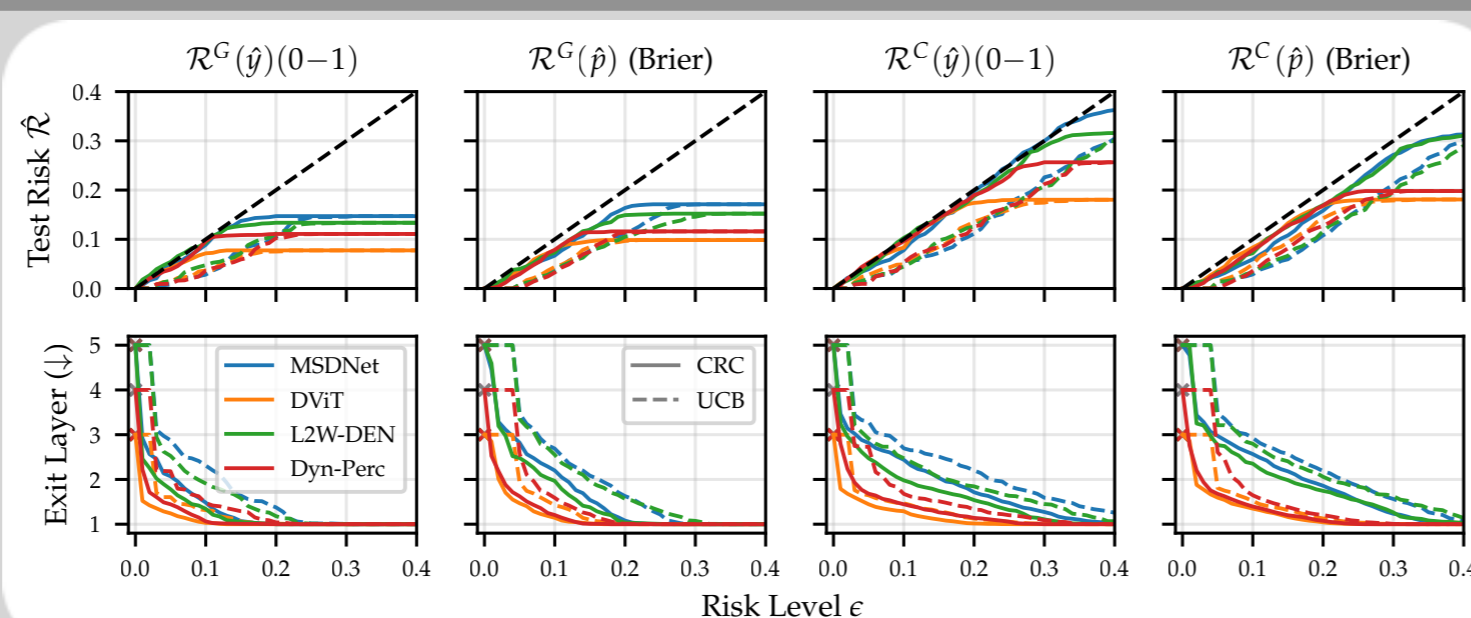
- Prediction control with task-specific losses
- Predictive distribution control with 'Brier score' loss
- Labelled and unlabelled data

## Experiments

- Verify that risk is controlled on test data, i.e.  $\hat{\mathcal{R}}(\hat{\lambda}; \mathcal{D}_{\text{test}}) \leq \epsilon$  (across multiple trials)
- Assess obtained efficiency gains in terms of average exit layer (across samples & multiple trials)

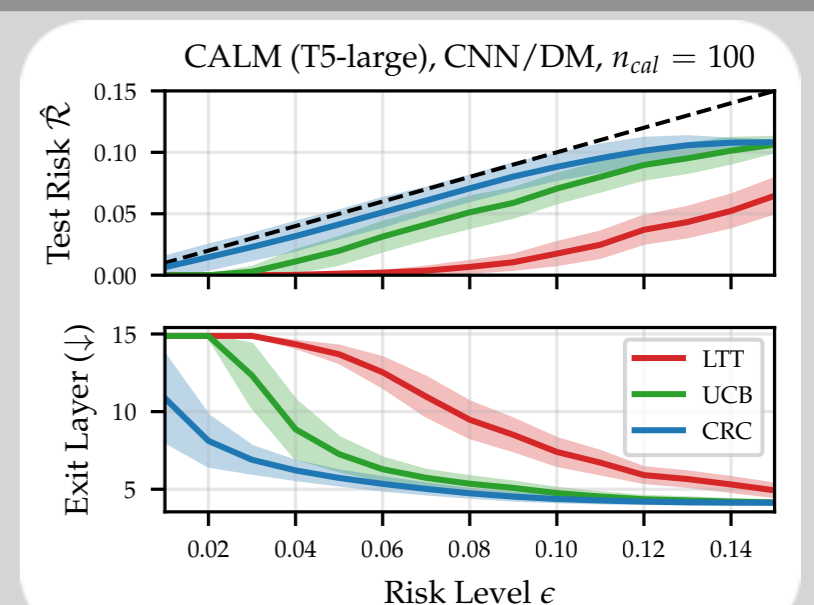
### Image Classification

- Generalizes across varying black-box early-exit architectures



### Language Modeling

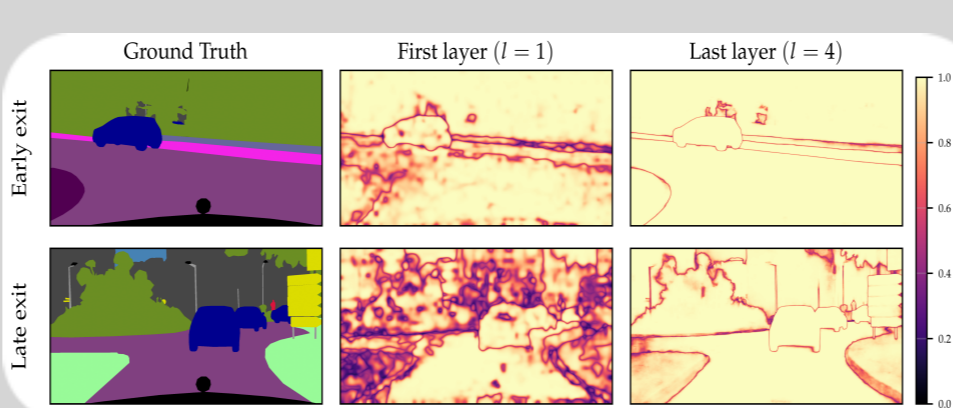
- Outperforms existing method Learn-then-Test (LTT) used by CALM



### Semantic Segmentation

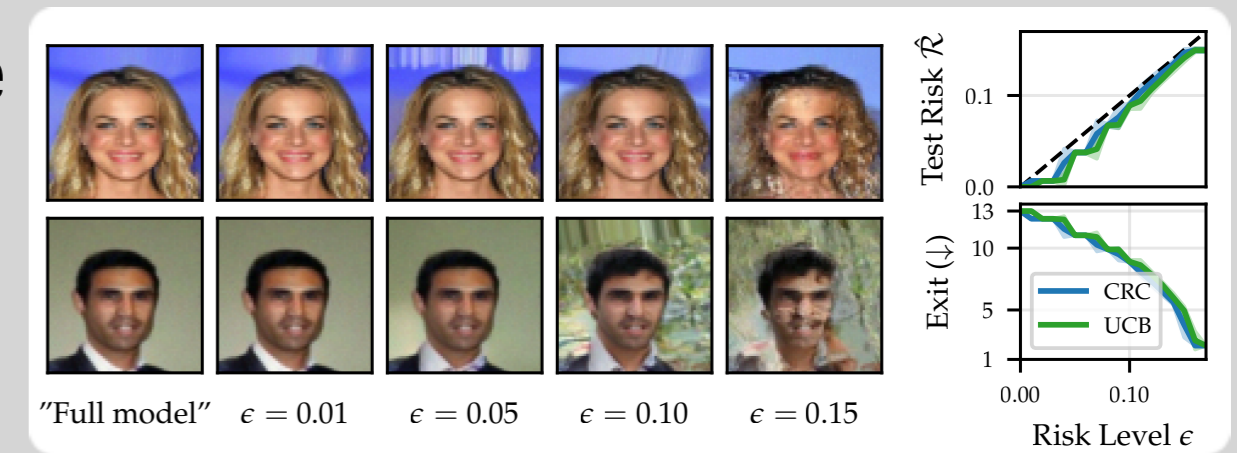
- Generalizes across varying confidence measures

Risk Level $\epsilon$	$\mathcal{R}^G(\hat{y})$ (mIoU)			$\mathcal{R}^G(\hat{p})$ (Brier)		
	0.01	0.05	0.1	0.01	0.05	0.1
Mean						
Top-1	6.3	33.7	53.5	0.0	13.6	43.4
Top-Diff	9.3	35.5	54.4	0.0	17.5	44.3
Entropy	5.2	36.0	54.3	0.0	17.9	41.0
Patch						
Top-1	10.0	35.7	53.3	0.0	18.4	45.3
Top-Diff	10.0	35.2	53.4	0.0	19.4	45.9
Entropy	9.1	34.8	53.5	0.0	18.0	45.8



### Image Generation

- Applicable to novel tasks (Diffusion)



## References

- Bates et al. (2021). Distribution-free, risk-controlling prediction sets (JACM)
- Angelopoulos et al. (2024). Conformal Risk Control (ICLR)
- Angelopoulos et al. (2021). Learn then Test: Calibrating Predictive Algorithms to Achieve Risk Control (Preprint)
- Schuster et al. (2022). Confident Adaptive Language Modeling (NeurIPS)